# Rotational and Translational Dynamics of N-Butyl-N-methylpiperidinium Trifluoromethanesulfonimide Ionic Liquids Studied by NMR and MD Simulations

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Supporting Information

ABSTRACT: Translational and rotational dynamics of the room temperature ionic liquid N-butyl-N-methylpiperidinium trifluoromethanesulfonimide, [C<sub>4</sub>mpip]- $[Tf_2N]$ , were investigated by <sup>1</sup>H, <sup>19</sup>F, and <sup>13</sup>C nuclear magnetic resonance (NMR) spectroscopy and molecular dynamics (MD) simulation. <sup>1</sup>H NMR and MD results for the temperature-dependent diffusion coefficients, D, spin-lattice relaxation times,  $T_1$ , and rotational correlation times,  $\tau_c$  for each site in the cation of  $[C_4 mpip]$  [Tf<sub>2</sub>N] are in good agreement. The  $T_1$  data indicate a long N–CH<sub>3</sub> group rotation time, comparable to the overall molecular reorientation time. Correlation time comparisons between 1-butyl-3-methylimidazolium RTILs with different anions  $(Cl^{-}, PF_{6}^{-}, Tf_{2}N^{-})$  argue against invoking hydrogen bond interactions between the N-CH<sub>3</sub> hydrogens and the electron rich center of the anion as an explanation of the



long N-CH<sub>3</sub> rotation times. Correlation time comparisons between piperidinium and pyrrolidinium RTILs with a common anion  $(Tf_2N^-)$  suggest that correlation times for N-CH<sub>3</sub> rotation are primarily a function of the local structure of the cation.

## **1. INTRODUCTION**

Room temperature ionic liquids (RTILs) are solely composed of ions, the key feature that imbues RTILs with a unique suite of properties, inter alia, high ionic conductivity, thermal and chemical stability, nonflammability, and nonvolatility.<sup>1</sup> Changes in the structure of the cation or anion lead to significant variations in these properties. The rational design of new RTILs is essential for task-specific applications. The characterization of rotational and translational motion is important for designing and exploring the properties of new RTILs. Piperidinium-based RTILs have received attention due to their superior thermal and electrochemical stability, properties which are important in electrochemical devices such as lithium-ion batteries and supercapacitors.<sup>2,3</sup> The rotational and translational motion of various RTILs have been investigated by NMR spectroscopy<sup>4-9</sup> and classical MD simulations<sup>5,10-12</sup> to understand the relationship between macroscopic properties and the molecular or atomic level dynamics of the RTILs. In this work, the translational and rotational motions of N-butyl-N-methylpiperidinium trifluoromethanesulfonimde,  $[C_4mpip][Tf_2N]$ , were investigated by <sup>1</sup>H and <sup>19</sup>F pulsed field-gradient NMR (PFG-NMR) and <sup>1</sup>H and <sup>13</sup>C spin-lattice relaxation  $(T_1)$  measurements, respectively. MD simulations were performed to provide theoretical insight into the experimental dynamics measurements.

## EXPERIMENTAL SECTION

Sample Preparation. [C<sub>4</sub>mpip][Tf<sub>2</sub>N] was prepared by anion exchange of [C4mpip][Br] which was synthesized from the reaction of N-methyl piperidine with butyl bromide according to literature procedures.<sup>2</sup> Trace moisture was removed by heating the sample in the NMR tube at 80 °C under 0.5 Torr vacuum until the water signal was not detectable by NMR (1-2 days). Samples of 1-butyl-3-methylimidizolium trifluoromethanesulfonimide, [C4mim][Tf2N], and N-butyl-Nmethylpyrrolidinium trifluoromethanesulfonimide,  $[C_4 mpyr]$ - $[Tf_2N]$ , were synthesized by standard methods and dried under a vacuum to a water-free state prior to the NMR measurements. Samples of 1-butyl-3-methylimidizolium hexafluorophosphate,  $[C_4 mim][PF_6]$ , and 1-butyl-3-methylimidizolium bromide, [C4mim][Br], were purchased from Sigma-Aldrich and dried before use.

NMR Experiments. NMR measurements were performed on a 9.4 T Bruker Avance NMR spectrometer at Larmor frequencies of 400.1, 376.4, and 100.6 MHz for <sup>1</sup>H, <sup>19</sup>F, and <sup>13</sup>C, respectively. Sample temperature was set with a Bruker BVT3000 temperature controller using a resistance heater in the probe, air for the heat transfer gas for high temperature, and N<sub>2</sub> gas evaporated directly from a liquid nitrogen dewar for low temperature. Sample temperatures were calibrated with 100%

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ethylene glycol and 100% methanol for temperatures above and below 300 K, respectively, according to the Bruker temperature calibration manual. All spectra were acquired on neat liquids in an unlocked mode.  $T_1$  was measured by the inversion recovery (180°- $\tau$ -90°-acquire) pulse sequence.<sup>13</sup>

Diffusion coefficients were measured using the stimulated echo bipolar pulse-gradient pulse (stebpgp) sequence. The gradient strength, g, was varied in 16 equal steps from 2 to 95% of the maximum gradient strength of the probe,<sup>14</sup> 54.4  $\pm$  0.3 G/cm, determined by a <sup>1</sup>H magnetic resonance imaging method.<sup>15</sup> The data were fit to  $S(g) = S(0) \exp[-D(\gamma \delta g)^2 (\Delta - \delta/3)]$ . In this equation, S(g) and S(0) are the echo heights at gradient g and 0, respectively, D is the diffusion coefficient,  $\gamma$  is the gyromagnetic ratio of nucleus investigated (<sup>1</sup>H, <sup>19</sup>F, as appropriate),  $\delta$  is the gradient-pulse length, and  $\Delta$  is the duration between the two gradient pulses.<sup>14</sup> To eliminate sample convection effects induced by temperature gradients along the z (gradient) axis in measurements above 330 K, the sample height was restricted to 1 mm in a Microtube (Shigemi Inc., Japan).  $\delta$  was fixed at 16 ms, and  $\Delta$  was varied to optimize the decay of the echo height at maximum gradient strength.

The rotational correlation times,  $\tau_{c}$  at each resolved site of the cation of  $[C_4mpip][Tf_2N]$  were calculated from <sup>1</sup>H and <sup>13</sup>C  $T_1$  data, independently. The <sup>1</sup>H  $T_1$  data were fit to the Bloembergen–Purcell–Pound (BPP) equation<sup>16</sup>

$$\frac{1}{T_1} = \frac{6}{5} \left(\frac{\mu_0}{4\pi}\right)^2 \frac{\gamma^4 \hbar^2}{b^6} I(I+1) \\ \times \left[\frac{\tau_c}{1+\omega_0^2 \tau_c^2} + \frac{4\tau_c}{1+4\omega_0^2 \tau_c^2}\right]$$
(1)

where  $\gamma$  is the gyromagnetic ratio of the proton  $(2.675 \times 10^8 \text{ rad/T} \cdot \text{s})$ ,  $\hbar$  is reduced Planck's constant,  $b (=\Sigma r)$  is the distance between protons and the sum runs over all protons that are dipolar coupled to the proton evaluated, I is the nuclear spin number of the proton (=1/2),  $\omega_0 = 2\pi\nu_0$ , where  $\nu_0$  is the proton observe frequency (400.1 MHz at 9.4 T), and  $\tau_c$  is the rotational correlation time.  $T_1$ 's are determined as a function of temperature. Where a minimum in the  $T_1$  vs T curve is observed, the relation  $\omega_0 \tau_c = 0.616$  is valid,  $\tau_c$  is calculated as 2.45  $\times 10^{-10}$  s/rad, and the *b* term can be evaluated as the only unknown in eq 1.<sup>16</sup> The distance term is assumed constant as a function of temperature and used to calculate  $\tau_c$  from  $T_1$  data taken at different temperatures.

The  ${}^{1}\text{H}-{}^{13}\text{C}$  dipole–dipole interaction is the dominant spin–lattice relaxation mechanism for  ${}^{13}\text{C}$  nuclei directly bonded to hydrogen. The equation for spin–lattice relaxation by heteronuclear dipolar relaxation can be written as<sup>7</sup>

$$\frac{1}{T_{\rm I}} = \frac{N}{10} \left(\frac{\mu_0}{4\pi}\right)^2 \frac{\gamma_{\rm H}^2 \gamma_{\rm C}^2 \hbar^2}{r^6} \left[ \frac{\tau_{\rm c}}{1 + (\omega_{\rm H} - \omega_{\rm C})^2 \tau_{\rm c}^2} + \frac{3\tau_{\rm c}}{1 + \omega_{\rm C}^2 \tau_{\rm c}^2} + \frac{6\tau_{\rm c}}{1 + (\omega_{\rm H} - \omega_{\rm C})^2 \tau_{\rm c}^2} \right]$$
(2)

where *N* is the number of protons directly bonded to carbon,  $\gamma_{\rm H}$  and  $\gamma_{\rm C}$  are the gyromagnetic ratio of the proton and the carbon, respectively, *r* is the distance between the carbon and the proton, and  $\omega_{\rm H}$  and  $\omega_{\rm C}$  are the angular NMR frequencies of the proton and the carbon, respectively. For the <sup>13</sup>C nucleus (*I* = 1/2),  $\gamma = 6.726 \times 10^7$  rad/T·s, and the observe frequency is  $\nu_0 = \omega_0/2\pi = 100.6$  MHz at 9.4 T. The evaluation of  $\tau_{\rm c}$  from <sup>13</sup>C  $T_1$  data using eq 2 does not require the observation of a  $T_1$  minimum to evaluate the distance term, r, which is fixed at the nominal C–H bond distance (1.09 Å). Equation 2 incorporates the approximation that dipolar relaxation is determined through the directly attached protons (N = 1, 2, and 3 for CH, CH<sub>2</sub>, and CH<sub>3</sub>, respectively). Discrimination against next nearest neighbor protons relies on the inverse sixth power distance dependence of the dipolar interaction.

The measured correlation time monitored at the N–CH<sub>3</sub> resonance reflects contributions from molecular reorientation and rotation about the N–CH<sub>3</sub> bond. The N–CH<sub>3</sub> rotation rate,  $1/\tau_{\rm NCH_3'}$  can be separated from the rate for molecular reorientation using the approximation  $1/\tau_{\rm c} \approx 1/\tau_{\rm R} + 1/\tau_{\rm NCH_3'}$  where  $\tau_{\rm c}$  is the effective correlation time measured at the N–CH<sub>3</sub> site and  $\tau_{\rm R}$  is the overall molecular reorientation time given by  $\tau_{\rm c}$  of the ring carbons.<sup>17</sup> The correlation time plots (Figures 3b and 4b) show two values for the N–CH<sub>3</sub> resonances,  $\tau_{\rm c}$  from eq 1 or 2 (unfilled circles) and  $\tau_{\rm NCH_3}$  if (filled circles). In this paper,  $\tau_{\rm NCH_3}$  specifically refers to the correlation time for rotation about the N–CH<sub>3</sub> bond derived through this approximation.

MD Simulation. All MD simulations were implemented with the Lucretius package using APPLE&P (Atomistic Polarizable Potential for Liquids, Electrolytes, & Polymers) force fields developed by Borodin,<sup>11</sup> in which polarizability terms were included. It has been reported that polarizable force fields predict the properties of molecules more accurately than nonpolarizable models.<sup>18</sup> The time step of 1 fs was used to integrate the equation of motion with a spherical cutoff of 10.5 Å in nonbonded van der Waals interactions. Long-range electrostatic interactions were treated using Ewald summation. A system consisting of 150 ion pairs was adopted at 1 atm. All bonds were constrained using the SHAKE method.<sup>19</sup> Periodic boundary conditions were applied in three dimensions. The system was equilibrated in the isothermal-isobaric (NPT) ensemble for 4 ns followed by 6-10 ns production runs at varying temperatures. Coordinates stored every 1 ps were used for the analysis.

The atomic diffusion coefficients were calculated at various temperatures with the Einstein relationship (3).

$$D = \lim_{t \to 0} \frac{1}{6t} \langle [r_i(t) - r_i(0)]^2 \rangle$$
(3)

After linear fitting of the mean square displacement (MSD), the diffusion coefficient is obtained from the fitted slope divided by 6. The rotational autocorrelation functions (RACFs) are computed using the protocol of Borodin et al.<sup>12</sup> RACFs were computed with eq 4

$$P_{\rm I}(t) = \langle \vec{e}(t) \cdot \vec{e}(0) \rangle \tag{4}$$

where  $\vec{e}(0)$  is the initial unit vector lying along the C–H bond and  $\vec{e}(t)$  is the same C–H unit vector at time *t*. The RACF is then fitted to the Kohlrausch–Williams–Watts (KWW) equation (eq 5),<sup>12</sup> yielding a curve. The rotational correlation time is then obtained as the integral from 0 to infinity of the fitted curve.

$$P_{\rm KWW}(t) = A \, \exp\left[-\left(\frac{t}{\tau_{\rm KWW}}\right)^{\beta}\right] \tag{5}$$

The apparent activation energy for translational and rotational motion was also computed.

## RESULTS AND DISCUSSION

**Diffusion Coefficient (D).** The structures and numbering system of the molecules used in this work are collected in Scheme 1. The <sup>1</sup>H and <sup>13</sup>C NMR spectra of  $[C_4mpip][Tf_5N]$ 

Scheme 1. Structure, Designation, and Numbering for Ionic Liquids



are presented in Figure 1a and b, respectively. Due to molecular symmetry, the resonances of H(2)/H(6), H(3)/H(5), C(2)/C(6), and C(3)/C(5) have equivalent chemical shifts.

The <sup>1</sup>H spectrum of the cation presents six resolved resonances. Each has been used independently to measure the diffusion coefficient, D, shown in the Arrhenius plot, Figure 2a. The average D is presented. The symbol used to indicate the data points is larger than the error bars representing one standard deviation. D of the anion obtained from monitoring the <sup>19</sup>F resonance is also plotted in this figure. The D values of  $[C_4mpip]^+$  and  $[Tf_2N]^-$  are nearly coincident over the temperature range, with the cation consistently showing a slightly greater D than the anion. Estimates of the hydrodynamic radius,  $r_{\rm s}$ , for the ions from MD predict greater diffusivity for the anion, but these estimates do not account for the shape of the ions. The inset of Figure 2a shows the linear relationship of D with  $T/\eta$  predicted by the Stokes-Einstein theory of diffusion, i.e.,  $D = k_{\rm B}T/6\pi\eta r_{\rm s}$ , where  $k_{\rm B}$  is the Boltzmann constant, T is the absolute temperature,  $\eta$  is the

viscosity, and  $r_s$  is the hydrodynamic radius of the molecule. The Arrhenius plot of *D* is fit to the Vogel–Fulcher–Tamman (VFT) equation,  $D = D_0 \exp[-B/(T - T_0)]$ , where  $D_0$ , *B*, and  $T_0$  are adjustable parameters which take the values 4.4 (±0.2) × 10<sup>-9</sup> m<sup>2</sup>/s, 654 ± 16 K, and 195 ± 1.5 K, respectively.

MD simulation results for cation diffusion are presented in Figure 2b and compared with the curve for the experimental data. The MD values are in good agreement with the magnitude of the experimental D's. The MD prediction does not capture the curvature in the Arrhenius plot, presenting a linear response with a slope matching that of the experimental data in the high temperature region. This difference may be caused by a combination of several factors, e.g., the APPLE&P force field used in this MD simulation and the time scale discrepancy between the NMR experiment and that for the simulation. The time scale for the NMR measurement is in the range of microseconds to milliseconds, while in the MD simulation the time length used for the MSD calculation is approximately 6 ns. However, the linear diffusive regime where the MSD increases linearly with time indicates that the simulation is sufficiently long enough to capture the magnitude of the diffusion coefficients. For ionic liquids in a glassy state encountered at low temperature, the force field is not suitable for predicting properties. The MD calculations are restricted to the high temperature region.

The activation energy,  $E_a$ , for translational diffusion for  $[C_4\text{mpip}]^+$  was calculated from the Arrhenius equation,  $D = D_0 \exp(-E_a/RT)$ , where  $D_0$  is the fitting parameter, R is the gas constant, and T is the absolute temperature. The  $E_a$  calculated from temperature dependent D obtained from <sup>1</sup>H PFG-NMR data is 33.8 ± 1.7 kJ/mol for T > 305 K and 54.0 ± 2.8 kJ/mol for T < 305 K. The latter value is similar to the larger  $E_a$  observed for 1,2-dimethyl-3-propylimidazolium trifluoromethanesulfonimide at low temperature.<sup>7</sup> The  $E_a$  calculated from the MD simulated D is 32.2 ± 1.3 kJ/mol, in good agreement with the  $E_a$  found in the high temperature region from the NMR measurement (see Figure 2b).

The translational correlation time for  $[C_4\text{mpip}]^+$  can be calculated from *D* through the relation  $\tau_{\text{trans}} = 2a^2/D$ , where the radius, *a*, calculated from the MD volume, is 0.35 nm and  $D = 4 \times 10^{-12} \text{ m}^2/\text{s}$  at 300 K.<sup>16</sup> For  $[C_4\text{mpip}]^+$ ,  $\tau_{\text{trans}}$  is 60 ns, more than 2 orders of magnitude longer than the correlation times for molecular reorientation ( $\approx 100 \text{ ps}$ ) where optimum overlap



Figure 1. (a) The <sup>1</sup>H NMR spectrum of  $[C_4mpip][Tf_2N]$ . (b) The <sup>13</sup>C NMR spectrum of  $[C_4mpip][Tf_2N]$ . The inset shows the boxed region in expanded form. The numbers on the resonances correspond to the positions identified on the structure.



**Figure 2.** (a) Temperature dependent diffusion coefficient (*D*) of the cation,  $[C_4mpip]^+$ , and anion,  $[Tf_2N]^-$ , in  $[C_4mpip][Tf_2N]$  measured by <sup>1</sup>H and <sup>19</sup>F PFG-NMR, respectively. The inset plots *D* of  $[C_4mpip]$  and  $[Tf_2N]$  in semilogarithmic scale as a function of  $T/\eta$ . Viscosity data are taken from the literature.<sup>32</sup> The fitted line in the main figure uses the VTF equation,  $D = D_0 \exp(-B/T - T_0)$  (see text). (b) The MD simulated temperature dependence of *D* of the cation and anion of  $[C_4mpip][Tf_2N]$ . The fitted line from part (a) is superposed on the data for comparison.



**Figure 3.** (a) <sup>1</sup>H  $T_1$  temperature dependence of  $[C_4\text{mpip}][Tf_2N]$ . The vertical lines denote the crystallization (left) and melting (right) temperatures for  $[C_4\text{mpip}][Tf_2N]$ . (b) Rotational correlation times calculated from the temperature dependence of <sup>1</sup>H  $T_1$  of  $[C_4\text{mpip}][Tf_2N]$ . The dotted line marks  $\tau_c = 0.245$  ns, the time determined by the Larmor frequency of the protons in the NMR experiment performed at 9.4 T ( $\omega_0 \tau_c \approx 0.616$ ) at  $T_{1\text{mim}}$ . With our estimate of  $\tau_{\text{NCHy}}$  the dipolar modulation frequency for N–CH<sub>3</sub> rotation (see text) is the slowest of any rotational motion, becoming equal to the Larmor frequency at the highest temperature.

between the NMR Larmor frequency and  $1/\tau_c$  occurs ( $\omega_0 \tau_c \approx 1$ ). Consequently, dipolar fluctuation from translational motion is not an effective spin-lattice relaxation mechanism at the temperatures used in this work.

**Rotational Correlation Time** ( $\tau_c$ ). <sup>1</sup>*H*  $T_1$ . The temperature dependence of <sup>1</sup>H  $T_1$  and  $\tau_c$  for  $[C_4 mpip][Tf_2N]$  is shown in Figure 3a and b, respectively. The resonance bands, assigned in Figure 1a, show clear  $T_{1\min}$  at temperatures higher than the melting point,  $T_{\rm m}$ . The <sup>1</sup>H  $T_1$  values for the ring sites, including H(7), average  $0.35 \pm 0.02$  s (300 K), indicating the isotropic motion approximation for the ring is justified.  $T_1$  values increase along the side chain toward the methyl terminus, a manifestation of increasing motion about sequential single bonds, i.e., segmental motion. From the  $T_1$  of the ring protons (0.35 s), the N-CH<sub>3</sub> relaxation time for a "static methyl group", i.e., a methyl group whose internal rotation rate is slow compared to overall molecular reorientation, is estimated to be 0.17 s.<sup>20</sup> Rapid internal motion can attenuate the dipolar coupling strength through a diminution in the spectral density function. For the specific case of a methyl group undergoing rapid internal rotation (relative to the molecular reorientation

time), the limiting reduction in the spin-lattice relaxation rate is 1/4,<sup>20,21</sup> i.e., the  $T_1$  is lengthened a factor of 4 over the value for a static methyl group. The  $T_1$  for such a methyl group is expected to be 0.68 s at 300 K. The measured N–CH<sub>3</sub>  $T_1$  of 0.34 s has a value between these limits, reflecting some degree of hindered rotational motion.

The correlation times derived from the  $T_1$  data are shown in Figure 3b. Above room temperature,  $\tau_c$  for the ring protons is linear with temperature. This is good evidence that a single motion dominates the relaxation of these protons. This motion is associated with overall molecular reorientation of the molecule. At low temperature,  $\tau_c$  for the N–CH<sub>3</sub> resonance (unfilled circles) approaches  $\tau_c$  for the ring resonances. From these correlation times, the N–CH<sub>3</sub> rotation time,  $\tau_{\rm NCH_3}$  can be obtained (see the Experimental Section). The  $\tau_{\rm NCH_3}$  values, shown by the filled circles in the high temperature region, are marginally longer than the overall molecular reorientation time.

<sup>13</sup>C  $T_1$ . The temperature dependence of <sup>13</sup>C  $T_1$  and  $\tau_c$  for  $[C_4mpip][Tf_2N]$  is shown in Figure 4a and b, respectively. The  $T_1$  values recorded at room temperature (300 K) are displayed



**Figure 4.** (a) <sup>13</sup>C  $T_1$  temperature dependence of  $[C_4mpip][Tf_2N]$ . The dashed lines indicate the crystallization (left) and melting temperature (right). (b) Rotational correlation times,  $\tau_{C}$ , calculated from the temperature dependence of  $T_1$  of <sup>13</sup>C NMR in the high temperature region. (c) Summary of the <sup>13</sup>C  $T_1$  (s) and  $\tau_C$  (ps) values at room temperature (300 K). For N–CH<sub>3</sub>,  $\tau = \tau_{NCH_3}$ .

on the structural formula (Figure 4c). The ring carbon  $T_1$  values cluster in a tight group  $(0.19 \pm 0.02 \text{ s})$  in apparent confirmation of the isotropic approximation.<sup>22</sup>  $T_1$  values of the side chain carbons show the ordering expected for segmental motion, i.e.,  $T_1$  increasing monotonically along the chain toward the methyl end. This order is clearly demonstrated by the correlation times in Figure 4b. The chain end methyl, C(10), and the trifluoromethyl resonance of the anion (not shown) do not show a  $T_{1\text{min}}$  over the investigated temperature range. At 300 K, the N–CH<sub>3</sub>  $T_1$  will vary between 0.13 s for a static methyl to 1.2 s for a rapidly rotating methyl ( $\tau_{\text{NCH}_3} \ll \tau_c$ ).<sup>22</sup> The high temperature of the  $T_{1\text{min}}$  for the N–CH<sub>3</sub> resonance, similar to the ring sites, and its  $T_1$  value (0.37 s) attest to the slow N–CH<sub>3</sub> rotation rate.

Correlation times are shown in Figure 4b for  $\tau_c$  (unfilled circles) and  $\tau_{\rm NCH_3}$  (filled circles) for the N–CH<sub>3</sub> resonance.  $\tau_{\rm NCH_3}$  is marginally shorter than  $\tau_c$  for the ring. Slow motional character of the N–CH<sub>3</sub> group is demonstrated in both the <sup>1</sup>H and <sup>13</sup>C data. Correlation times calculated from <sup>13</sup>C  $T_1$  measurements are shorter than those from <sup>1</sup>H data, typically a factor of 2–4, but in some cases an order of magnitude. The discrepancy in the values has been pointed out previously, and possible reasons for this have been advanced.<sup>23</sup> Part of the difference arises from differences in actual C–H bond lengths and the bond length value of 1.09 Å used in the NMR estimate (eq 2). A 2–3% difference in the C–H bond length can generate a factor of 2 error in the correlation time calculated from <sup>13</sup>C  $T_1$  data, plotted as a function of inverse temperature, are shown in Figures 2S–5S in the Supporting Information, where it is clear that the MD calculations align better with the <sup>1</sup>H data. The MD-generated  $\tau_c$ 's capture the trends of the experimental data well.

The correlation times of  $[C_4mpip]^+$  in  $[C_4mpip][Tf_2N]$ , computed by MD simulation, are presented in Figure 5. The result shows the proton or carbon in the terminal methyl exhibits the shortest  $\tau_c$  followed by those in N-methyl, alkyl chain, and the ring, i.e., the order observed in the NMR measurements. The short rotational correlation times of the



Figure 5. The rotational correlation times of  $[C_4mpip][Tf_2N]$  as a function of temperature from MD simulations.



Figure 6. (a) Anion-carbon radial distribution functions (RDF) of  $[C_4mpip][Tf_2N]$  at 300 K. (b) RDF of oxygen in the anion relative to hydrogen in the cation at 300 K.

side chain are the result of greater flexibility, i.e., increased degrees of motional freedom, of the side chain carbons compared to the ring.<sup>8</sup> Slower reorientation of the ring is explained by its larger inertial mass relative to the terminal carbon(s) of the side chain.

It has been noted that N-CH<sub>3</sub> rotation in imidazolium RTILs is slow, and arguments invoking hydrogen bond interactions have been advanced to rationalize these rates.<sup>24,25</sup> Evidence for the presence of hydrogen bonding is also obtained from the MD simulations. The strong electrostatic interaction between the piperidinium ring and the anion is shown by the ion-ion radial distribution function (RDF), g(r), in Figure 6S (Supporting Information). The cation-anion RDF demonstrates that the cation-anion is closely packed due to electrostatic attraction compared to the relatively loosely packed cation-cation and anion-anion. To explore which part of the cation exhibits the strongest interaction with the anion, the RDFs of the center of mass of the anion relative to the individual carbons of the cation were computed (Figure 6a). The side chain terminal carbon C(10) has the lowest probability for close approach to the anion, attributed to its nonpolarity and long distance from the cation center. The N-CH<sub>3</sub> carbon is closest to the anion followed by the aminomethylene carbons of the piperidinium ring, C(2) and C(6). The high probability of the anion to interact with Nlinked carbons (C(11), C(2) and C(6), C(7)), especially with the axial N-CH<sub>3</sub> group, is the consequence of the strong electrostatically driven approach of the ions. These carbons and their attached hydrogens are present at the interface of the ion pair by structural definition. The hydrogen bonds between O of the anion and H of the aminocarbon fragments are inferred from the RDFs of Figure 6b which exhibit shortest O-H distances of approximately 2.5 Å. O…H-C distances of this magnitude, and larger, that exceed the sum of the van der Waals O and H radii do not meet the criteria of the classical definition of the hydrogen bond but nevertheless fall within the modern, broad definition for weak hydrogen bonds.<sup>26</sup>

In contrast to the view that hydrogen bonding is causal to slow N–CH<sub>3</sub> rotation rates, the long  $\tau_{\rm NCH_3}$  may arise from the electronic and geometric structure inherent in the cation. This case is supported by the following experimental argument. If the N–CH<sub>3</sub> rotation rate is significantly slowed by specific interactions between the N–CH<sub>3</sub> protons and the heteroatoms of the anion, the N–CH<sub>3</sub> rotation rate should vary as a function

of the anion. If the rotation rate is determined primarily by cation structure constraints, the rotation rates should be independent of the nature of the anion. This general argument is expected to be applicable to both imidazolium-based and tetraalkylammonium-based ILs containing N-CH<sub>3</sub> groups. In this work, we measured temperature dependent  $T_1$ 's for  $[C_4 mim][Tf_2N]$  and use  $T_1$  data from the literature for  $[C_4 \text{mim}][PF_6]^{24}$  and  $[C_4 \text{mim}][Br]^{27}$  Since it is highly unlikely that anions as varied as  $Br^-$ ,  $PF_6^-$ , and  $Tf_2N^-$  will have similar hydrogen bonding affinities, comparisons in this series should present a fair test if hydrogen bonding is important. Representative  $T_1$  and  $\tau_c$  data for  $[C_4mim][Tf_2N]$  and  $[C_4 mim][PF_6]$  are shown in Figures 7S and 8S in the Supporting Information. Since these RTILs have different viscosities, the  $au_{
m NCH_2}$  values are compared between RTILs which have the same overall molecular reorientation time. Experimentally, we use  $\tau_c$  for C(2) to represent this value and compare the three RTILs at the temperature at which the C(2) $\tau_{\rm c}$  is 100 ps. Since  $\tau_{\rm c} = 4\pi \eta a^3/3kT$ ,<sup>16</sup> this prescription holds  $\eta/T$ constant, and if the Debye radius, a, remains constant, i.e., if there is no specific association of the anion and cation,  $\tau_{\rm NCH}$ , should be constant within the series. The  $\tau_{\rm NCH_3}$  value of the cation in combination with the  $[Tf_2N]^-$ ,  $[PF_6]^-$ , and  $[Br]^$ anion is 14, 13, and 12 ps, respectively, i.e.,  $13 \pm 1$  ps. This variation, less than 10%, is comparable to the estimated error in the  $T_1$  measurement. On this criterion, the slow N-CH<sub>3</sub> rotation rate is independent of the anion. Hydrogen bonding interactions with the N-CH3 group must be associated with a low activation energy and short ( $\approx 1$  ps) hydrogen bond lifetime in comparison to the N-CH<sub>3</sub> rotation correlation time of 10 ps. These two phenomena, N-CH<sub>3</sub> rotation and hydrogen bond formation, are not correlated. Any effect that might be ascribed to hydrogen bonding from the anion must be subtle, within the 10% error of the N–CH<sub>3</sub> rotation times.<sup>28</sup> Infrared spectroscopic evidence for the presence of hydrogen bonds in these ILs has been reported,<sup>29,30</sup> but the existence of long-lived hydrogen bonds is not supported by our data. The NMR criterion does not rule out weak hydrogen bond interactions.

Slow N–CH<sub>3</sub> rotation is observed in the tetraalkylammonium-based RTIL series.<sup>31</sup> Arguments invoking hydrogen bonds have been advanced to explain slow N–CH<sub>3</sub> rotation in  $[C_4mpip][Tf_2N]$ .<sup>24</sup> The  $\tau_{\rm NCH_3}$  values of  $[C_4mpip][Tf_2N]$  and  $[C_4mpyr][Tf_2N]$  allow us to compare rotation rates in structurally similar cations where the anion is kept constant. The <sup>13</sup>C  $T_1$  data on which these comparisons depend are shown in Figure 4a and Figure 9S (Supporting Information), respectively. These cations are based on six-membered (piperidine) and five-membered (pyrrolidine) rings (Scheme 1) that will present significant differences in intramolecular steric interactions with substituents at the cation center. The first order prediction is that N-CH<sub>3</sub> rotation rates should be different if the controlling effect is intramolecular in origin. As above, the comparison is made with the ring  $\tau_c$  set at 100 ps, i.e., at ca. 310 K for [C<sub>4</sub>mpip][Tf<sub>2</sub>N] and 270 K for  $[C_4mpyr][Tf_2N]$ .  $\tau_{NCH_3}$  of these RTILs differ by a factor of 3, 46, and 150 ps for  $[C_4mpip]^+$  and  $[C_4mpyr]^+$ , respectively, demonstrating that N-CH<sub>3</sub> rotation rates are sensitive to cation structure.

## CONCLUSION

Translational and rotational dynamics of  $[C_4mpip][Tf_2N]$  were investigated by <sup>1</sup>H, <sup>19</sup>F, and <sup>13</sup>C nuclear magnetic resonance (NMR) spectroscopy and molecular dynamics (MD) simulations. The NMR  $T_1$  data indicate slow internal N-CH<sub>3</sub> rotation rates, similar to overall molecular reorientation. MD simulations reproduce the trends seen in translational and rotational motion of [C<sub>4</sub>mpip][Tf<sub>2</sub>N] and are in close agreement with the proton derived experimental correlation times. Correlation time comparisons in the imidazolium, piperidinium, and pyrrolidinium IL series indicate that long  $\tau_{\rm NCH_2}$  is primarily a function of cation structure. Hydrogen bond interactions between the N-CH<sub>3</sub> hydrogens of the cation and the oxygen atoms of the anion do not play a significant role in slowing N-CH<sub>3</sub> rotation rates. The long correlation time observed for N-CH<sub>3</sub> rotation may have its origin in the CN bond length, typically 4% shorter than aliphatic CC bond distances. This common structural feature explains the generality of the observation over an array of cation structures and hard and soft anions.

## ASSOCIATED CONTENT

#### **S** Supporting Information

Figures 1S–9S show (1) the temperature dependence of *D* for long and short sample lengths, (2–5) reorientational correlation time comparisons from <sup>1</sup>H, <sup>13</sup>C, and MD for each resolved site in  $[C_4mpip]+$ , (6) ion–ion center of mass distribution of  $[C_4mpip][Tf_2N]$ , (7, 8) temperature dependent <sup>13</sup>C  $T_1$  and rotational correlation times of select sites in  $[C_4mim][Tf_2N]$  and  $[C_4mim][PF_6]$ , respectively, and (9) temperature dependence of the <sup>13</sup>C  $T_1$  and rotational correlation time of  $[C_4mpyr][Tf_2N]$ . This material is available free of charge via the Internet at http://pubs.acs.org.

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#### Notes

The authors declare no competing financial interest.

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## The Journal of Physical Chemistry C

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